

Objectives

- Learn about and apply the following to solve problems
 - Visualisation
 - Backtracking
 - Data mining
 - Heuristics
 - Performance modelling
 - Pipelining

Writing algorithms

- One of the oldest known algorithms was written by Euclid over 2000 years ago
- It's designed to find the greatest common divisor of two numbers (the largest number which divides both of them)



FUCLIDES



The GCD algorithm

- Suppose x and y represent two whole numbers
- Euclid's algorithm goes like this:

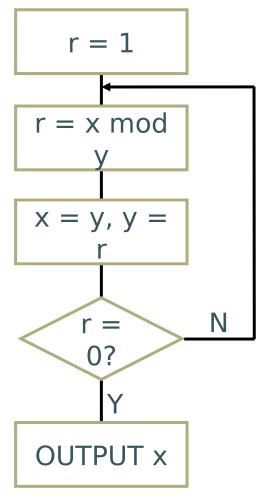
```
r = 1
WHILE r <> 0
    r = x mod y
    x = y
    y = r
ENDWHILE
OUTPUT y
```

- A flowchart is a visualisation of an algorithm
 - Draw a flowchart of this algorithm



The GCD algorithm

 Test the algorithm by tracing the values of r, x and y starting with x = 420, y = 66





The GCD algorithm

 Test the algorithm by tracing the values of r, x and y starting with x = 420, y = 66

| r | X | У | |
|----|-----|----|--|
| 1 | 420 | 66 | |
| 24 | 66 | 24 | |
| 18 | 24 | 18 | |
| 6 | 18 | 6 | |
| 0 | 6 | 0 | |

Output is 6



Visualising an algorithm

 An image is much easier for a human to understand than a table of numbers

What does the graph represented below look

like?

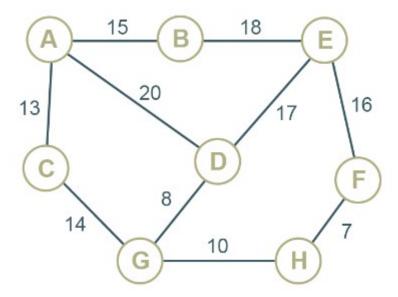
| | Α | В | С | D | Е | F | G | Н |
|---|----------------------------|--------|--------|--------|--------|--------|--------|--------|
| А | | 1 5 | 1 3 | 2 | | | | |
| В | 1 5 | | | | 1 8 | | | |
| С | 1 5 1 3 2 0 | | | | | | 1 4 | |
| D | 2 | | | | 1 7 | | 8 | |
| Е | | 1 8 | | 1 7 | | 1 6 | | |
| F | | | | | 1 6 | | | 7 |
| G | | | 1 4 | 8 | | | | 1 0 |
| | | | | | | | 1 | |



The graph

Here it is visualised as a set of nodes and

edges



 The weights on the edges could be distances or costs

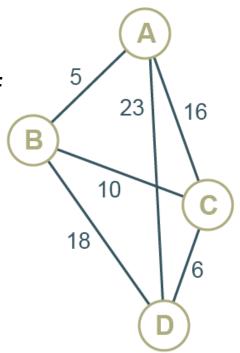


Shortest path algorithm

 Suppose we wanted to find the shortest path from city A to city D

 One method would be to perform an exhaustive search of all possible routes

- With 4 cities, how many possible routes are there?
 - What is the shortest route?





Exhaustive search

• With 4 cities, there are $3 \times 2 = 6$ possible routes

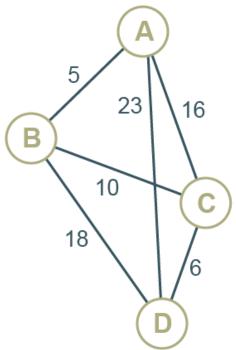
With 5 cities, there are 4 x 3 x 2
The sportest route from A

 The shortest route from routes to D is A

B
C
D, a
 distance of 21

 With only 4 cities, an exhaustive search is possible

But what if there are 8 cities?





Exhaustive search

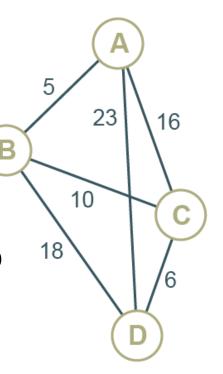
 The formula for the number of possible routes for 8 cities is:

$$7! = 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 = 211,680$$

• The number of possible routes for $\frac{B}{10}$ cities is $\frac{10!}{3,628,800}$

 Clearly a better algorithm needs to be found

 We'll use an algorithm to find the shortest distance from A to D





Backtracking

 One technique is backtracking, whereby you go some way along one route and then backtrack to see if there is a better route

 Starting at A, visit B, C and D to see which is the shortest distance

 B is shortest, so backtrack to A, travel to B and from there visit C and D

A
$$\square$$
 B \square C is 5 + 10 = 15
A \square B \square D is 5 + 18 = 23

- The shortest path so far is A □ B □ C = 15
- Backtrack to C. A [] B [] C [] D = 15 + 6 =
 21



23

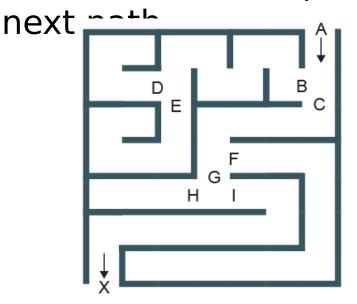
10

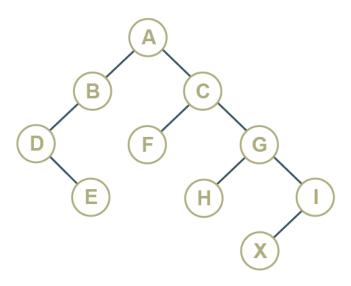
18

16

Solving mazes

- A maze can be represented as a graph
- A depth-first traversal is used to explore a path until a dead-end is reached, and then it backtracks to the previous node, and tries the







Worksheet 6

- Try the first question in **Task 1** of Worksheet 6
 - If you have time, try the second one too





Can it be solved?

- Sometimes it is not possible to find a solution to a problem in a reasonable time
- Cracking a strong password may be impossible using an exhaustive search





Cracking a password

 What other methods, apart from an exhaustive search taking 34 thousand years, could you try to discover someone's password or crack a code?



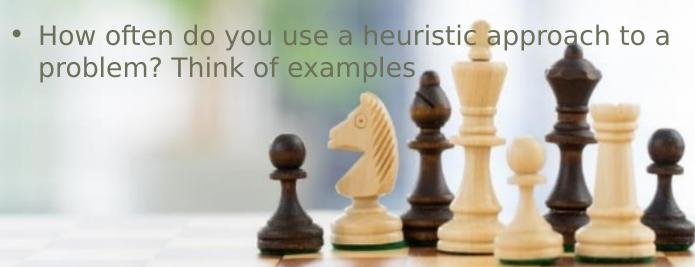
Educated guess?

- To crack a password, you could try guesswork based on the person's family, names, birthdates, favourite team, etc.
- You could try comparing it with words in a dictionary
- To crack a code, if you had a large chunk of encrypted text, you could use a frequency analysis of letters – for example 'e' is the commonest letter in English, followed by 't'



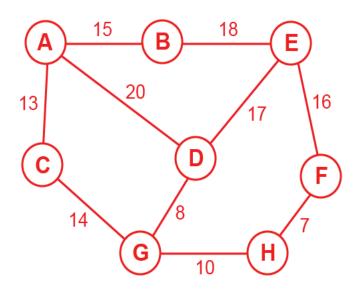
Heuristic methods

- Heuristic methods include 'rules of thumb', educated guesses, intuitive judgements or common sense
- Teachers, students, psychologists, chess players, use heuristics to solve problems



An intractable problem

- The Travelling Salesman Problem (TSP) is a problem which cannot be completely solved
- The problem is to find the shortest route which visits every city and returns to the start





Heuristic methods

- A heuristic method is used to rapidly find a solution that is 'good enough', even though it might not be the optimal solution
- Many algorithms have been invented to provide a heuristic solution to the Travelling Salesman Problem (TSP)
 - The best heuristic solutions are within 2-3% of the optimal solution for up to 85,000 cities or nodes



Applications of heuristic methods

- The heuristic approach is used in many applications such as
 - routing messages across the Internet
 - building circuit boards
 - transportation
 - virus checking
 - DNA analysis
 - artificial intelligence



Data mining

- Data mining is the process of collecting and then analysing huge amounts of data
- Many organisations such as the National Health Service, police, Google, Amazon and supermarkets collect billions of bytes of data about people
- They can then analyse or 'mine' the data to find connections and associations
- A range of modelling techniques are used to help to identify patterns in the data



Applications of data mining response rates to marketing campaigns by being able to target them more

- Anticipating resource demands
- Detecting fraud and cybersecurity issues

accurately to the needs of each customer

Finding connections between seemingly unconnected events

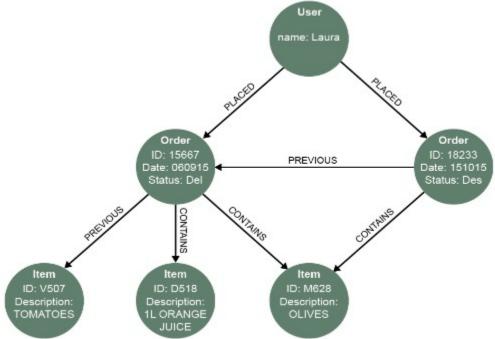
Big data

- The term big data is often used in connection with data mining
- It implies that huge amounts of data are collected and stored
- It is defined by three major features, known as the 3Vs: Volume, Variety and Velocity
- Parallel computing, in which algorithm tasks are executed concurrently on a cluster of machines or supercomputers, is fundamental to managing big data tasks



Mining supermarket data

 A supermarket can customise their advertising and special offers, depending on your purchase history or that of other customers who





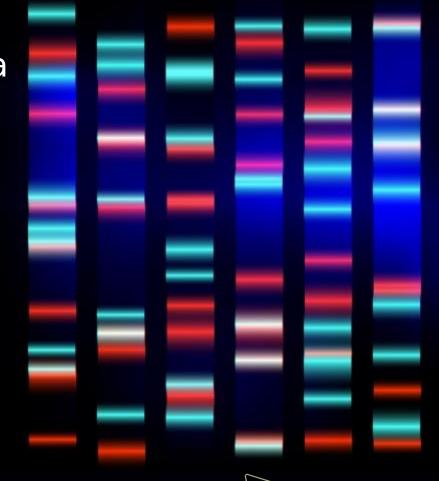
Amazon data mining

 Amazon make recommendations based on what other readers who have read the same books as you have also read



Medical applications of data mining

 Data mining and big data techniques are widely used in the public health field, discovering new patterns among population groups using social media data





Performance modelling

- How efficient is your algorithm?
- One measure of efficiency is the Big-O notation (covered in Section 12)
- This measures the suitability of algorithms in terms of execution time and space
- You can time different algorithms using builtin timer functions
 - The performance of some algorithms deteriorates so rapidly as the problem size increases that they are not usable

Performance of sorting algorithms

- Sorting algorithms vary enormously in their efficiency
- The bubble sort is the slowest of the wellknown algorithms
- The quicksort is very fast for a large number of items

Worksheet 2

Now try Task 2 in the worksheet



Pipelining

- Pipelining is an implementation technique where multiple instructions are overlapped in execution
- Instructions enter the 'pipeline' at one end, and at each stage part of the instruction is completed and moves to the next stage while another instruction enters the pipeline – rather like an assembly line



Pipelining in PCs

- Pipelining is now commonplace in PCs
- Intel chips can execute many instructions simultaneously to achieve high processing speeds of 3GHz and more



Plenary

- You should be able to explain and give examples of
 - visualisation
 - backtracking
 - heuristics
 - data mining
 - performance modelling
 - pipelining

and say how they are used in solving problems



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